



Designation: D7905/D7905M – 19

Standard Test Method for Determination of the Mode II Interlaminar Fracture Toughness of Unidirectional Fiber-Reinforced Polymer Matrix Composites¹

This standard is issued under the fixed designation D7905/D7905M; the number immediately following the designation indicates the year of original adoption or, in the case of revision, the year of last revision. A number in parentheses indicates the year of last reapproval. A superscript epsilon (ϵ) indicates an editorial change since the last revision or reapproval.

1. Scope

1.1 This test method covers the determination of the mode II interlaminar fracture toughness, G_{IIc} , of unidirectional fiber-reinforced polymer matrix composite laminates under mode II shear loading using the end-notched flexure (ENF) test (Fig. 1).

1.2 This method is limited to use with composites consisting of unidirectional carbon-fiber- and glass-fiber-reinforced laminates. This limited scope reflects the experience gained in round robin testing. This test method may prove useful for other types and classes of composite materials; however, certain interferences have been noted (see Section 6).

1.3 The values stated in either SI units or inch-pound units are to be regarded separately as standard. The values stated in each system are not necessarily exact equivalents; therefore, to ensure conformance with the standard, each system shall be used independently of the other, and values from the two systems shall not be combined.

1.3.1 Within the text the inch-pound units are shown in brackets.

1.4 *This standard does not purport to address all of the safety concerns, if any, associated with its use. It is the responsibility of the user of this standard to establish appropriate safety, health, and environmental practices and determine the applicability of regulatory limitations prior to use.*

1.5 *This international standard was developed in accordance with internationally recognized principles on standardization established in the Decision on Principles for the Development of International Standards, Guides and Recom-*

mendations issued by the World Trade Organization Technical Barriers to Trade (TBT) Committee.

2. Referenced Documents

2.1 ASTM Standards:²

- D792 Test Methods for Density and Specific Gravity (Relative Density) of Plastics by Displacement
- D883 Terminology Relating to Plastics
- D2584 Test Method for Ignition Loss of Cured Reinforced Resins
- D2734 Test Methods for Void Content of Reinforced Plastics
- D3171 Test Methods for Constituent Content of Composite Materials
- D3878 Terminology for Composite Materials
- D5229/D5229M Test Method for Moisture Absorption Properties and Equilibrium Conditioning of Polymer Matrix Composite Materials
- D5687/D5687M Guide for Preparation of Flat Composite Panels with Processing Guidelines for Specimen Preparation
- D7264/D7264M Test Method for Flexural Properties of Polymer Matrix Composite Materials
- E4 Practices for Force Verification of Testing Machines
- E6 Terminology Relating to Methods of Mechanical Testing
- E122 Practice for Calculating Sample Size to Estimate, With Specified Precision, the Average for a Characteristic of a Lot or Process
- E177 Practice for Use of the Terms Precision and Bias in ASTM Test Methods
- E456 Terminology Relating to Quality and Statistics
- E691 Practice for Conducting an Interlaboratory Study to

¹ This test method is under the jurisdiction of ASTM Committee D30 on Composite Materials and is the direct responsibility of Subcommittee D30.06 on Interlaminar Properties.

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² For referenced ASTM standards, visit the ASTM website, www.astm.org, or contact ASTM Customer Service at service@astm.org. For *Annual Book of ASTM Standards* volume information, refer to the standard's Document Summary page on the ASTM website.

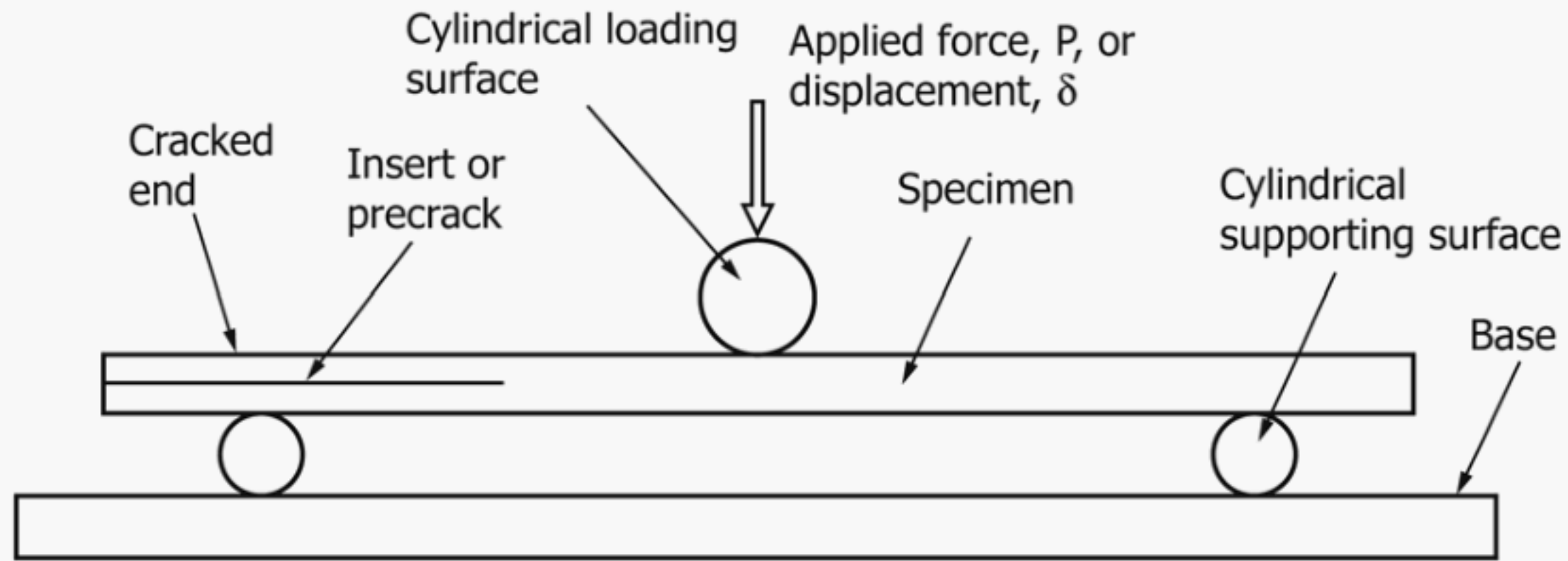


FIG. 1 ENF Test Fixture and Specimen Nomenclature

Determine the Precision of a Test Method

E1309 Guide for Identification of Fiber-Reinforced Polymer-Matrix Composite Materials in Databases (Withdrawn 2015)³

E1434 Guide for Recording Mechanical Test Data of Fiber-Reinforced Composite Materials in Databases (Withdrawn 2015)³

E1471 Guide for Identification of Fibers, Fillers, and Core Materials in Computerized Material Property Databases (Withdrawn 2015)³

3. Terminology

3.1 Terminology **D3878** defines terms relating to high-modulus fibers and their composites. Terminology **D883** defines terms relating to plastics. Terminology **E6** defines terms relating to mechanical testing. Terminology **E456** and Practice **E177** define terms relating to statistics. In the event of conflict between terms, Terminology **D3878** shall have precedence over the other terminology standards.

NOTE 1—If the term represents a physical quantity, its analytical dimensions are stated immediately following the term (or letter symbol) in fundamental dimension form, using the following ASTM standard symbology for fundamental dimensions, shown within square brackets: $[M]$ for mass, $[L]$ for length, $[T]$ for time, $[u]$ for thermodynamic temperature, and $[nd]$ for non-dimensional quantities. Use of these symbols is restricted to analytical dimensions when used with square brackets, as the symbols may have other definitions when used without the brackets.

3.2 Definitions of Terms Specific to This Standard:

3.2.1 *compliance calibration (CC) method*—the method of data reduction where the relationship between specimen compliance $[T^2/M]$ and delamination length $[L]$ is determined prior to testing by measuring specimen compliance $[T^2/M]$ at multiple simulated delamination lengths.

3.2.2 *mode II interlaminar fracture toughness, G_{IIc} $[M/T^2]$* —the critical value of strain energy release rate, G , $[M/T^2]$ for delamination growth $[L]$ due to an in-plane shear force $[M/T^2]$ or displacement $[L]$ oriented perpendicular to the delamination front.

3.2.3 *non-precracked (NPC) toughness $[M/T^2]$* —an interlaminar fracture toughness value that is determined from the preimplanted insert.

3.2.4 *precracked (PC) toughness $[M/T^2]$* —an interlaminar fracture toughness value that is determined after the delamination has been advanced from the preimplanted insert.

3.2.5 *strain energy release rate, G $[M/T^2]$* —the loss of strain energy, dU $[ML^2/T^2]$, in the test specimen per unit of specimen width $[L]$ for an infinitesimal increase in delamination length, da $[L]$, for a delamination growing self-similarly under constant displacement $[L]$; in mathematical form,

$$G = -\frac{1}{B} \frac{dU}{da} \quad (1)$$

where:

U = total elastic strain energy in the specimen;

a = delamination length; and

B = specimen width.

3.3 Symbols:

A —intercept of the linear fit of compliance versus crack length cubed data

a —delamination length

a_{calc} —crack length calculated from an unloading curve after the NPC test

a_i —insert length in the trimmed specimen

a_j —the j^{th} crack length used during compliance calibration ($j = 1, 2$)

a_o —delamination length used in fracture test

a_{PC} —actual crack length used during the PC test

a_{vis} —visually determined crack length after the NPC test

B —specimen width

C —specimen compliance

C_o —specimen compliance during load-up of the fracture test (see Figure 6 in 13.1)

C_u —specimen compliance from unloading after the non-precracked test

δ —displacement of loading roller during testing perpendicular to the plane of the specimen (Fig. 1)

E_{If} —flexural modulus of the specimen

G —total strain energy release rate

G_{IIc} —mode II interlaminar fracture toughness

³ The last approved version of this historical standard is referenced on www.astm.org.

G_Q —candidate mode II interlaminar fracture toughness
 $\%G_Q$ —peak percentage of G_Q achieved during compliance calibration
 h —specimen half-thickness (Fig. 2)
 L —specimen half-span (Fig. 2)
 L_c —distance from the center of the support roller at the cracked end of the specimen to the cracked end of the specimen (Fig. 2)
 L_u —distance from the center of the support roller at the uncracked end of the specimen to the uncracked end of the specimen (Fig. 2)
 m —slope of the linear fit of compliance versus crack length cubed data
 P —force applied to center loading roller and perpendicular to the plane of the specimen (Fig. 1)
 P_c —critical force for mode II fracture
 P_f —the compliance calibration force used at crack length a_i
 P_{Max} —maximum value of force on the force-displacement curve
 r_1 —radius of the loading roller (Fig. 2)
 r_2 —radius of the support rollers (Fig. 2)
 r^2 —correlation coefficient of linear fit of compliance versus crack length cubed
 Δs —maximum measured difference in crack length along the delamination front of the precrack
 U —total elastic strain energy in the specimen

4. Summary of Test Method

4.1 The ENF specimen shown in Fig. 1 consists of a rectangular, uniform thickness, unidirectional laminated composite specimen containing a non-adhesive insert at the mid-plane that serves as a delamination initiator. Forces are applied to the specimen through an ENF fixture under displacement controlled loading.

4.2 Delamination growth is not stable in the ENF test. A method is presented so that the initiation values of the mode II interlaminar fracture toughness are obtained from the preimplanted insert as well as from a precrack.

4.3 A record of the applied force versus center roller displacement is to be obtained using an x-y recorder or equivalent real-time plotting device, or else it may be obtained and stored digitally. The mode II interlaminar fracture

toughness, G_{IIc} , is obtained using the compliance calibration (CC) method. This is the only acceptable method of data reduction for this test (1).⁴

4.4 This standard recommends that static mode II precracking is performed and a recommended method is described. Other precracking methods may be used provided that a record of the shape of the precracked delamination front is obtained prior to the PC test. Precracking methods that typically leave crack front markings for post-test evaluation of these values include mode I and fatigue mode II.

5. Significance and Use

5.1 Susceptibility to delamination is one of the major design concerns for many advanced laminated composite structures. Knowledge of a laminated composite material's resistance to interlaminar fracture is useful for product development and material selection. Furthermore, a measurement of the mode II interlaminar fracture toughness that is independent of specimen geometry or method of force introduction is useful for establishing design allowables used in damage tolerance analyses of composite structures. Knowledge of both the non-precracked and precracked toughnesses allows the appropriate value to be used for the application of interest.

5.2 This test method can serve the following purposes:

5.2.1 To establish quantitatively the effect of fiber surface treatment, local variations in fiber volume fraction, and processing and environmental variables on G_{IIc} of a particular composite material;

5.2.2 To compare quantitatively the relative values of G_{IIc} for composite materials with different constituents;

5.2.3 To compare quantitatively the values of G_{IIc} obtained from different batches of a specific composite material, for example, to use as a material screening criterion or to develop a design allowable; and

5.2.4 To develop delamination failure criteria for composite damage tolerance and durability analyses.

⁴ The boldface numbers in parentheses refer to the list of references at the end of this standard.

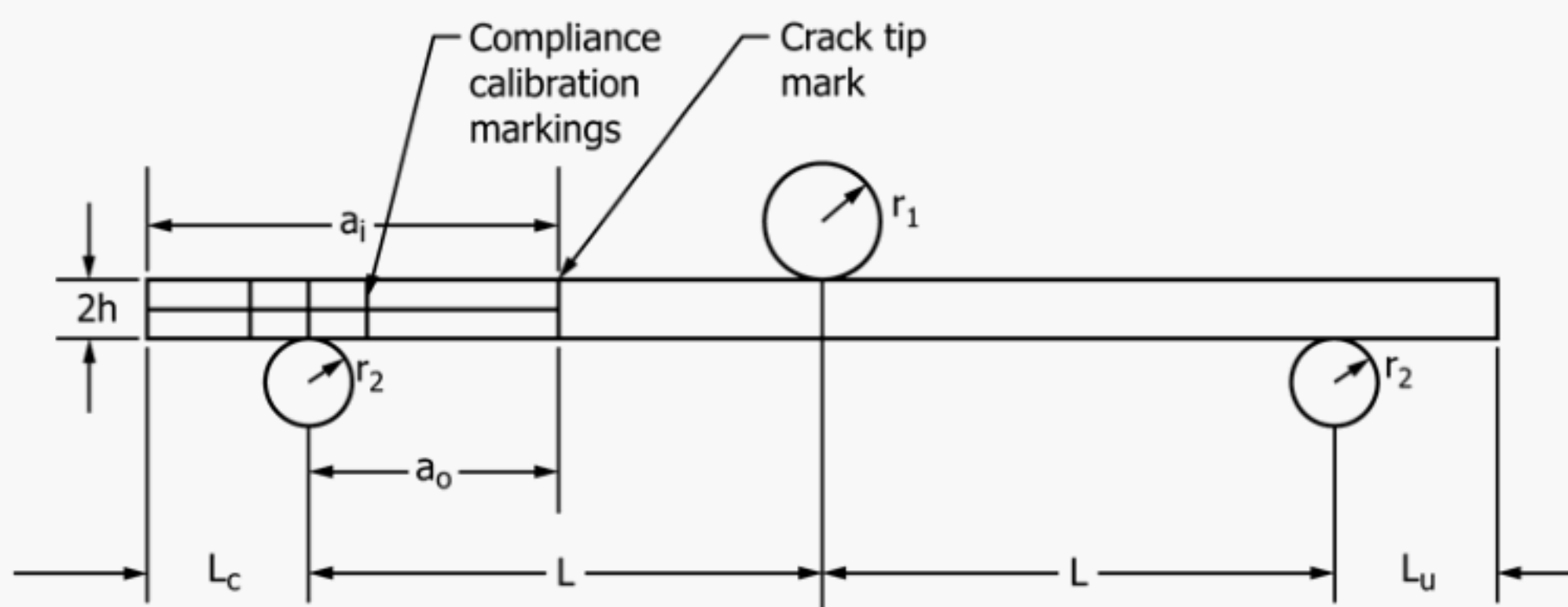


FIG. 2 ENF Specimen, Fixture, and Dimensions

6. Interferences

6.1 Linear elastic behavior is assumed in the calculation of G used in this method. This assumption is valid when the zone of damage or nonlinear deformation at the delamination front, or both, is small relative to the smallest specimen dimension, which is typically the specimen's thickness for the ENF test.

6.2 G_{IIC} is obtained for both non-precracked and precracked specimens based on the maximum load point. G_{IIC} based on the nonlinear load point or other measures, such as a compliance offset, may also be obtained if desired. However, definitions of this type have not been related to any specific physical occurrences in the ENF test.

6.3 The three loading noses in the ENF test fixture may be fixed, rotatable, or rolling. Fixed loading noses or pins supported in a v-groove are recommended, and loading noses of this type were used in the interlaboratory test program that was conducted in support of this standard. The type of supports that are used is to be reported as described in Section 14. The loading noses should uniformly contact the specimen across its width. Lack of uniform contact can affect results, most commonly due to non-uniform loading across the width of the specimen. Formulas used in this standard assume a uniform line loading across the entire specimen width at the loading nose and at the specimen supports; deviations from this type of loading are beyond the scope of this standard.

6.4 There is an inherent error associated with the use of Eq 7 to obtain the calculated crack length, and it is not expected that the calculated crack length will exactly correspond to the true length of the precrack. However, since toughness is computed by CC, it has been shown (2) that this error in crack length will not affect the accuracy of the computed toughness provided that the recommended approach is followed.

6.5 For very tough composites, large deformations at the onset of delamination growth could affect the accuracy of the ENF test. For typical unidirectional glass and carbon reinforced unidirectional composites, it has been shown (1) that the combined effects of friction and geometric nonlinearities will affect the accuracy of the recommended approach by approximately 2.5 % or less for glass-reinforced polymer matrix composites with toughnesses up to 1.45 kJ/m² [8.28 in.-lbf/in.²] and by 3 % or less for polymer matrix composites with carbon reinforcement with toughnesses up to 2.10 kJ/m² [12.0 in.-lbf/in.²]. Testing of composites that exhibit greater toughness may produce somewhat larger errors. One means of checking for nonlinearities is to examine the difference between the nonlinear point and the maximum load point. If this is found to be greater than approximately 5 % of P_{Max} , further investigations may be in order to determine the reason for the discrepancy, for example, material nonlinearity, geometric nonlinearity, or subcritical crack advance. The results of this investigation may be used to choose a new test geometry, for example to eliminate geometric nonlinearities, or to choose a definition of critical load that is different from P_{Max} , for example in the case of subcritical crack advance.

6.6 A precracking method that only produces a short crack "jump," for example, by positioning a specimen with a crack

tip close to the center loading roller, may produce precracked toughness values that are significantly higher than those that will be produced for a long crack jump following the recommended procedure (2, 3).

6.7 The toughness measured using this method is sensitive to reinforcement volume and void content. Consequently, the test results may reflect manufacturing quality as much as material properties.

6.8 *Number of Points for CC*—The use of a three-point CC was studied extensively in References (2, 4) and resulted in the recommended approach (11.9). However, equivalent results will be obtained with a five-point CC, and one may use this approach following Note 4 (11.9).

6.9 The toughness values obtained by this test method for delamination growth at 0°/0° interfaces may not be representative of the toughness required for delamination growth at interfaces with different relative ply orientations.

7. Apparatus

7.1 *Testing Machine*—A properly calibrated test machine shall be used which can be operated in a displacement control mode with a constant displacement rate in the range from 0.025 to 1.6 mm/min [0.001 to 0.063 in./min]. The testing machine will conform to the requirements of Practices E4.

7.2 The testing machine shall be equipped with a loading fixture as shown in Fig. 1 and Fig. 2.

7.2.1 A fixture geometry with a nominal specimen span length ($2L$) of 100 mm [4 in.] and a nominal half-span length (L) of 50 mm [2 in.] is required.

7.2.2 The cylindrical loading surface shall have a radius, r_1 , in the range of 4.7 to 9.6 mm [0.185 to 0.378 in.]. The cylindrical supporting surfaces shall have the same radius, r_2 , which shall be in the range of 3.0 to 6.4 mm [0.118 to 0.250 in.]. The loading surface shall be centered between the two supporting surfaces (Fig. 2). All load and support surfaces shall be finely ground and free of indentation and burrs with all sharp edges relieved, with a hardness of 55 HRC or greater. Loading and support surfaces may be arranged in a fixed, rotatable, or rolling arrangement, where rotation may occur only about the cylindrical surfaces' center points as viewed in the orientation of Fig. 1 and Fig. 2. All other movement of the supporting surfaces shall be restrained, and loading surface shall only be free to move vertically when viewed in the orientation of Fig. 1 and Fig. 2 (that is, perpendicular to the plane of the specimen).

7.2.3 The system compliance, defined as the compliance of the load frame with the test fixture installed, shall be less than 3 % of the measured compliance of the specimens that are tested. The system compliance shall be determined by using an essentially rigid calibration bar with the ENF test fixture and a span length ($2L$) of 100 mm [4.0 in.]. It is recommended that the calibration bar is at least as stiff as a steel bar with a moment of inertia, I , equal to 6 cm⁴ [0.144 in.⁴]. When this is the case, the system compliance can be determined as the slope of the deflection versus force data from the test of the calibration bar in the ENF fixture. For calibration bars with a lower moment of inertia, the bar's compliance should be

accounted for. Here, the system compliance may be computed as the slope of the deflection versus force data from the test of the calibration bar minus the compliance of the calibration bar, defined as $L^3/(6EI)$, where L is the half-span length and E and I are the Young's modulus and moment of inertia, respectively, of the calibration bar. The system compliance shall then be compared to the minimum compliance from all specimens tested to ensure that the 3 % requirement is met. It is recommended that the system compliance tests be performed with a nominal loading rate of 0.05 mm/min [0.002 in./min], but rates in the range of 0.02 to 0.08 mm/min [0.0008 to 0.003 in./min] are acceptable.

7.2.4 The fixture cannot have rotational bearings that allow rotation about an axis parallel to the length direction of the specimen.

7.2.5 It is recommended that the test fixture be equipped with alignment features to ensure that (1) the loading and support rollers are parallel, and (2) the longitudinal direction of the specimen is perpendicular to the roller direction (3).

7.3 *Force Indicator*—The testing machine's force-sensing device shall be capable of indicating the total force carried by the test specimen. This device shall be essentially free from inertia-lag at the specified rate of testing and shall indicate the force with an accuracy over the force range(s) of interest of within ± 1 % of the indicated value. Forces are dependent on the specimen geometry and toughness. A method to calculate the expected forces can be found in Annex A1.

7.4 *Load Point Displacement Indicator*—The load point displacement may be obtained from the crosshead separation of the load frame provided that the compliance requirement of 7.2.3 is satisfied. Otherwise, the load point displacement shall be taken from a properly calibrated external gauge or transducer or a stiffer test fixture, or both, or load frame should be used, or both. The load point displacement indicator shall indicate the load point displacement with an accuracy of ± 1 % at the displacement at which delamination growth occurs.

7.5 *Force versus Load Point Displacement Record*—A digital record of force versus load point displacement shall be stored for subsequent post-processing.

7.6 *Micrometers and Calipers*—A micrometer with a 4 to 7 mm [0.16 to 0.28 in.] nominal diameter ball interface or a flat anvil interface shall be used to measure the specimen thickness. A ball interface is recommended for thickness measurements when at least one surface is irregular (for example, a coarse peel ply surface, which is neither smooth nor flat). A micrometer or caliper with a flat anvil interface shall be used for measuring length, width, and other machined surface dimensions. The use of alternative measurement devices is permitted if specified (or agreed to) by the test requestor and reported by the testing laboratory. The accuracy of the instrument(s) shall be suitable for reading to within 1 % of the specimen dimensions. For typical specimen geometries, an instrument with an accuracy of ± 0.0025 mm [± 0.0001 in.] is adequate for thickness measurements, while an instrument with an accuracy of ± 0.025 mm [± 0.001 in.] is adequate for measurement of length, width, and other machined surface dimensions.

8. Sampling and Test Specimens

8.1 *Sampling*—Test at least five specimens per test condition unless valid results can be gained through the use of fewer specimens, such as the case of a designed experiment. For statistically significant data, the procedures outlined in Practice E122 should be consulted. The method of sampling shall be reported.

8.2 *Specimen and Test Configuration*—Test laminates must contain an even number of plies and must be unidirectional, with delamination growth occurring in the 0° (zero degree) direction. Specimen dimensions shall conform to those presented in Fig. 3 and Fig. 4, which are chosen such that placement of the specimen within the fixture will be as defined in Table 1 and Fig. 2.

8.3 Manufacturing:

8.3.1 A flat composite plate shall be manufactured with a preimplanted non-adhesive film insert. Specimens are to be cut from these plates as shown in Fig. 3 and Fig. 4. Fabrication and machining are to be performed following Guide D5687/D5687M.

8.3.2 A non-adhesive film insert shall be implanted at the midplane of the laminate during layup to form an initiation site for the delamination (Fig. 3 and Fig. 4). The film thickness shall be no greater than 13 μ m [0.0005 in.]. A polymer film is recommended for the insert to avoid problems with folding or crimping at the cut end of the insert. For epoxy matrix composites cured at or below 177 $^\circ$ C [350 $^\circ$ F], a thin film made of polytetrafluoroethylene (PTFE) is recommended. For composites with polyimide, bismaleimide, or thermoplastic matrices that are manufactured at relatively high temperatures, that is, greater than 177 $^\circ$ C [350 $^\circ$ F], a thin polyimide film is recommended. If a polyimide film is used, the film shall be painted or sprayed with a mold release agent before it is inserted in the laminate. Caution should be used, as mold release agents containing silicone may contaminate the laminate by migration through the individual layers. It is often helpful to coat the film at least once and then bake the film before placing the film on the composite. This will help to prevent silicone migration within the composite. It also is often necessary to decohere the light bond that might form between the insert and the composite (2). For materials outside the scope of this standard, different film materials and procedures may be required.

8.3.3 The plate shall be made in such a way that the specimen dimensions presented in Fig. 3 and Fig. 4 may be achieved. Manufacturing large panels with a full-width insert in the center of the length direction is recommended to prevent thickness variations in the test specimens. After manufacture, these panels are cut width-wise along the centerline of the insert to create two plates, each with an edge view as shown in Fig. 3 and Fig. 4. A typical panel would be 400 mm [16 in.] long in the 0° direction with a 100 mm [4 in.] insert. Depending on the saw blade and amount trimmed at the edges, this will yield two plates that are approximately 200 mm [8 in.] long with an initial insert length (a_i) of approximately 50 mm [2 in.].

8.3.4 Prior to cutting the plate into specimens, the end of the insert should be accurately located and marked, and markings



- 4 ALL DIMENSIONS IN INCHES.

- 5 DRAWING INTERPRETATION PER ANSI
Y14.5-1982 AND ANSI/ASME B46.1-1966.

- 6 PLY ORIENTATION TOLERANCE TO 2°
RELATIVE TO -A-.

FIG. 4 Specimen—ENF Test (Inch-pound Units)

TABLE 1

Parameter	Value or Range
L	50 mm [2.0 in.]
L_c	≥ 15 mm [≥ 0.6 in.]
L_u	≥ 45 mm [≥ 1.8 in.] <i>when the same specimen is to be used for non-precracked and precracked testing.</i> <i>Otherwise:</i>
	≥ 15 mm [≥ 0.6 in.]
a_o	30 mm [1.2 in.]

a 0.5 mm [0.02 in.] diameter lead or smaller. The edges shall then be marked with three vertical compliance calibration markings, within the cracked region, at distances of 20, 30, and 40 mm [0.8, 1.2, and 1.6 in.] from the tip of the insert.

11.3.3 If specific gravity, density, reinforcement volume, or void volume, or combinations thereof, are to be reported, then obtain these samples from the same panels being tested. Specific gravity and density may be evaluated by means of Test Methods **D792**. Volume percent of the constituents may be evaluated by one of the matrix digestion procedures of Test Methods **D3171**, or, for certain reinforcement materials such as glass and ceramics, by the matrix burn-off technique of Test Method **D2584**. The void content equations of Test Method **D2734** are applicable to both Test Method **D2584** and the matrix digestion procedures.

11.4 *Test Environment*—If possible, test the specimen under the same fluid exposure level used for conditioning. However, cases such as elevated temperature testing of a moist specimen place unrealistic requirements on the capabilities of common testing machine environmental chambers. In such cases, the mechanical test environment may need to be modified, for example, by testing at elevated temperature with no fluid exposure control, but with a specified limit on time to failure from withdrawal from the conditioning chamber. Record any modifications to the test environment.

NOTE 3—When testing a conditioned specimen at elevated temperature with no fluid exposure control, the percentage moisture loss of the

specimen prior to test completion may be estimated by placing a conditioned traveler of known weight within the test chamber at the same time the specimen is placed in the chamber. The traveler should be configured to mimic the specimen, such that moisture evaporation is comparable to that of the test specimen. Upon completion of the test, the traveler is removed from the chamber, weighed, and the percentage weight calculated and reported.

11.5 The specimen shall be placed in the fixture so that its longitudinal direction is perpendicular to the loading rollers (see 7.2.5).

11.6 Loading for all CC and fracture tests shall be performed in displacement control at a nominal rate of 0.5 mm/min [0.02 in./min], although rates between 0.10 and 0.80 mm/min [0.004 to 0.031 in./min] are acceptable. Unless otherwise specified, unloading shall also be in displacement control at a rate between 0.10 and 1.6 mm/min [0.004 to 0.063 in./min].

11.7 Peak forces during CC are equal to 50 % of the expected value of the critical force (P_c) at that particular crack length; these are chosen to correspond to approximately 25 % of G_{IIc} . That is, the peak CC force varies with crack length. The method of determining the peak force for each crack length during CC is presented in Annex A2.

11.8 Compliance calibration tests are performed by loading the specimen to the peak CC force as defined in 11.7 and then unloading. The force and deflection data are to be recorded continuously or at frequent and regular intervals during the loading portion only; a sampling rate of 5 Hz or greater and a target minimum of 500 data points per test are recommended.

11.9 Values of G_{IIc} shall be obtained from the insert and from the precrack. All toughness values are obtained using the CC method. Subsection 11.9.1 is to be used if both NPC and PC toughness values are to be obtained from the same specimen and the recommended precracking procedure is to be adopted; otherwise, 11.9.2 and 11.9.3 are to be used. Peak forces expected during these fracture tests may be estimated by the method in Annex A1.

NOTE 4—If desired, a five-point CC may be used. In this case, CC is performed for both the NPC and PC tests with crack lengths, a , equal to 20, 25, 35, and 40 mm [0.8, 1.0, 1.4, and 1.6 in.], and the fracture test is still performed with $a = 30$ mm [1.2 in.]. Data from all five crack lengths are then used to obtain the CC coefficients (13.2).

11.9.1 *Non-Precracked and Precracked Toughness from the Same Specimen*—In the approach that follows, crack advance

during the NPC test creates the precrack that is used for the PC test. The approach has been shown to produce accurate NPC and PC toughnesses with a PC G_{IIc} that is within or approaching the “minimum toughness plateau” that some materials evidence, that is, when G_{IIc} decreases to a minimum plateau value with the amount of dynamic advance that occurs during precracking (2-4). The approach also ensures that any differences between the location of the true and calculated crack tip do not affect the accuracy of G_{IIc} (2).

11.9.1.1 *Non-Precracked CC*—With reference to Fig. 2, the specimen is placed in the fixture so that the CC mark that is farthest from the cracked end is aligned with the center of the support roller at the cracked end. The first CC test is then performed with a crack length, a , equal to 20 mm [0.8 in.], following the procedure defined in 11.8. The specimen is then repositioned such that $a = 40$ mm [1.6 in.], that is, so that the CC mark that is closest to the cracked end is aligned with the center of the support roller at the cracked end. The second CC test is then performed as defined in 11.8.

11.9.1.2 *Non-Precracked Fracture Test*—Following NPC CC, the specimen shall be repositioned in the fixture so that $a = 30$ mm. This shall correspond to placing the center CC mark over the center of the support roller that is at the cracked end. The specimen is then loaded until the delamination advances, as seen by visual assessment on the specimen or by a drop in force on the force versus displacement plot. The specimen shall be unloaded at a nominal rate of 0.5 mm/min [0.02 in./min], although rates between 0.10 and 0.80 mm/min [0.004 to 0.031 in./min] are acceptable (that is, in order to decrease the total time required for the test). The force and displacement data are to be recorded continuously or at frequent and regular intervals during the entire test; a sampling rate of 5 Hz or greater and a target minimum of 1000 data points per test are recommended.

11.9.1.3 *Determination of Crack Length for the Precracked Test*—The unloading data from the non-precracked fracture test of 11.9.1.2 is used to compute a value of a_{calc} using the method of 13.6. This value of a_{calc} is measured from the existing center CC mark. A new “PC crack tip mark” shall be placed at this location. Three new “PC CC markings” shall then be placed at 20, 30, and 40 mm [0.8, 1.2, and 1.6 in.] from the PC crack tip mark as shown in Fig. 5. The center mark, with distance from the crack tip equal to 30 mm [1.2 in.] is for the fracture test, and the other two marks are for CC testing.

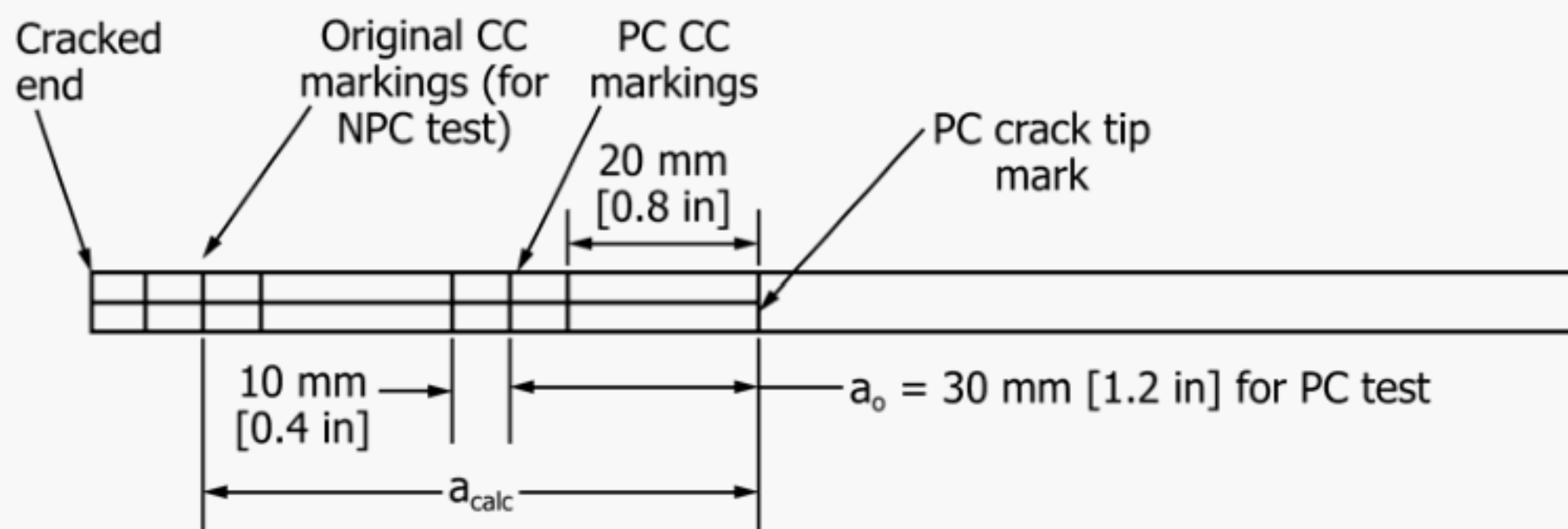


FIG. 5 Configuration of Specimen for Precracked Test When the Same Specimen is Used for NPC and PC Testing (Nominal Dimensions Shown)

If desired, the location of the crack tip may also be determined visually as the average of the locations found on the two edges. If the visually determined crack tip, a_{vis} , is (1) past (to the right of) the loading roller and (2) longer than a_{calc} , then a_{vis} may be used in place of a_{calc} for the placement of the PC crack tip mark.

11.9.1.4 Precracked CC—Prior to the PC fracture test, the compliances from two different crack lengths are obtained by appropriate placement of the specimen in the fixture. The first CC test is performed with $a = 20$ mm [0.8 in.] and the second with $a = 40$ mm [1.6 in.]. This is performed using the PC CC markings of 11.9.1.3 and following the procedure of 11.9.1.1.

11.9.1.5 Precracked Fracture Test—Following PC CC, the specimen shall be repositioned in the fixture so that $a = 30$ mm [1.2 in.]. This shall correspond to placing the center PC CC mark over the center of the support roller that is at the cracked end. The specimen is then loaded until the delamination advances, as seen by visual assessment on the specimen or by a drop in force on the force versus displacement plot. The specimen is then unloaded. The force and deflection data are to be recorded continuously or at frequent and regular intervals during the loading portion only; a sampling rate of 5 Hz or greater and a target minimum of 750 data points per test are recommended.

11.9.2 Non-Precracked Toughness Only—This test is performed as described in 11.9.1.1 and 11.9.1.2. Unloading data and determination of a_{calc} (11.9.1.3) are not required.

11.9.3 Precracked Toughness Only—The method that follows is valid provided that a record of the precracked delamination front shape prior to the PC test can be obtained. This record must be sufficiently detailed to allow for quantitative measurements of crack length as a function of position at five locations in the width direction. These five locations shall consist of the two edges, 50 % of the distance from either edge towards the center of the specimen, and in the specimen's center.

11.9.3.1 Subsequent to precracking and prior to testing, the location of the crack front is to be determined by an appropriate method and marked on the edge of the specimen. This comprises the “PC crack tip mark.”

11.9.3.2 Three “PC CC markings” shall be placed at distance of 20, 30, and 40 mm (0.8, 1.2, and 1.6 in.) from the PC crack tip mark.

11.9.3.3 The PC CC and PC fracture test are performed following the procedures for the NPC test and as specified in 11.9.2.

12. Validation

12.1 Values for toughness shall not be calculated for any specimen that fails by breaking in some manner other than delamination advance, such as breaking at some obvious flaw, unless such flaw constitutes a variable being studied. Retests shall be performed as needed to replace results from specimens where values are not calculated.

13. Calculations

13.1 Interlaminar Fracture Toughness Calculations—NPC and PC initiation values of G_{IIc} are to be obtained from the maximum force (P_{Max}) (Fig. 6).

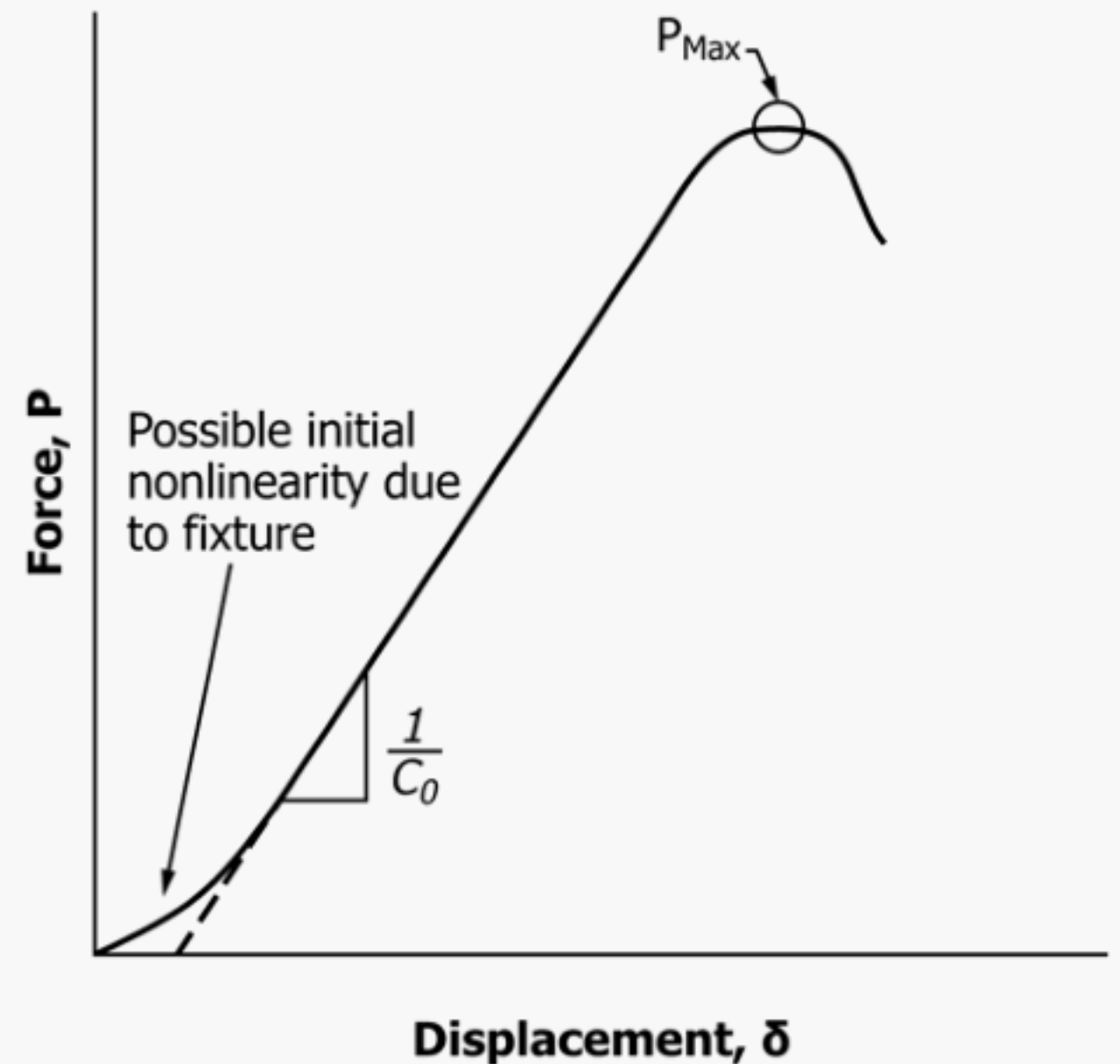


FIG. 6 Illustration of Compliance and Maximum Load Point Determination

13.2 Compliance Calibration Coefficients—CC coefficients from each NPC and PC test are to be determined using the method described in 13.2.1 and 13.2.2 (1, 2, 4).

13.2.1 Non-Precracked CC Coefficients—Plot the three compliances from the NPC test versus crack length cubed. The three compliances are those from the two CC tests (at $a = 20$ and 40 mm [0.8 and 1.6 in.]) and from the fracture test (C_0 , Fig. 6, which is at crack length $a_0 = 30$ mm [1.2 in.]). At each crack length, the compliance is determined by a linear least squares regression analysis to obtain the slope of the displacement versus force (δ versus P) data. For the two CC tests, this regression analysis (curve-fit) shall include all data for which the force is greater than or equal to 90 N [20 lb], including the peak force used during the test. The 90 N [20 lb] force is chosen to be sufficiently large such that the curve-fit excludes any data affected by an initial nonlinearity (Fig. 6). For the fracture test, the regression analysis (curve-fit) shall include all data for which the force is greater than or equal to 90 N [20 lb] and less than or equal to 50 % of the maximum force from the fracture test (this yields C_0). The CC coefficients, A and m , are to be determined using a linear least squares linear regression analysis of the compliance, C , versus crack length cubed (a^3) data of the form:

$$C = A + ma^3 \quad (2)$$

where A and m are the CC coefficients or, more specifically, A is the intercept and m is the slope obtained from the regression analysis. The correlation coefficient, r^2 , for the curve-fit is also to be determined. The linear least squares regression analysis used to determine the compliance at any crack length from the δ versus P data as well as the values of A , m , and r^2 is described in Annex A3.

13.2.2 Precracked CC Coefficients—PC CC coefficients are to be determined in the same fashion as the NPC CC

coefficients (13.2.1), except that the three compliances from the PC test and their associated crack lengths are to be used.

13.3 Determination of Candidate Toughness—A candidate toughness, G_Q , is first determined and checked for validity. If it is valid, then $G_{IIC} = G_Q$. Otherwise, the results from the test are discarded (in which case G_Q is generally used to modify the CC forces for subsequent testing). The NPC candidate toughness is determined using the method of 13.3.1. If the recommended precracking method of 11.9.1 is adopted, then the PC candidate toughness is determined identically. Otherwise, the PC candidate toughness is determined as described in 13.3.2.

13.3.1 Non-Precracked Tests, and Precracked Toughness Tests per 11.9.1—The candidate toughness is determined using

$$G_Q = \frac{3mP_{Max}^2a_o^2}{2B} \quad (3)$$

where m is the CC coefficient, P_{Max} is the maximum force from the fracture test as defined in 13.1, a_o is the crack length used in the fracture test (30 mm [1.2 in.]), and B is the specimen width. When determining the NPC G_Q , these parameters are taken from the NPC CC and fracture tests. They are taken from tests of the precracked specimen when determining the PC G_Q .

13.3.2 Precracking by a Method Other Than 11.9.1:

13.3.2.1 Crack Front Assessments—Following completion of the PC test, the actual crack lengths at the five widthwise locations specified in 11.9.3 shall be determined by suitable means, for example, from pre-test c-scan images, or if a precracking method is used that leaves visually evident crack front markings, by splitting the specimen in half and making appropriate measurements. The shortest of these five lengths shall be subtracted from the longest to determine Δs , a measure of deviation from straightness (2-4). The actual crack length used for the PC test, a_{PC} , shall be determined by the equivalent area method (3, 5). This method defines an area of growth equivalent to that which occurred, but with a straight front normal to the edges, and the location of this front defines the length of the crack. The method is employed by using the shape of the precrack to determine the area bounded by the delamination front, the two longitudinal edges, and the location of the support roller at the cracked end during the precracked test, and then dividing this area by the specimen's width.

13.3.2.2 The candidate toughness is determined using:

$$G_Q = \frac{3mP_{Max}^2a_{PC}^2}{2B} \quad (4)$$

13.4 Candidate Toughness Evaluation—The NPC candidate toughness is evaluated using the method of 13.4.1. If the recommended precracking method of 11.9.1 is adopted, then the PC candidate toughness evaluation is performed identically. Otherwise, the PC candidate toughness evaluation is performed as described in 13.4.2.

13.4.1 Non-Precracked Tests, and Precracked Toughness Tests per 11.9.1—The percentages of G_Q ($\%G_Q$) that were achieved during compliance calibration are calculated using:

$$\%G_{Q,j} = \left[\frac{100(P_j a_j)^2}{(P_{Max} a_o)^2} \right]; j = 1, 2 \quad (5)$$

where $\%G_{Q,j}$ are the two values of G_Q associated with the two compliance tests, P_{Max} is taken from the fracture test as defined in 13.1, P_j is the peak value of the force achieved during CC at a_j , and a_j is the j^{th} crack length used during CC. For each NPC and PC test, the two values of $\%G_Q$ are computed at $a_1 = 20$ mm [0.8 in.] and $a_2 = 40$ mm [1.6 in.]. If both values satisfy $15 \leq \%G_Q \leq 35$, then the candidate toughness is accepted. Otherwise, it is recommended that the results from this test are discarded and, if necessary, CC forces are modified appropriately for additional testing (2).

13.4.2 Precracking by a Method Other Than 11.9.1—The percentages of G_Q ($\%G_Q$) that were achieved during PC compliance calibration are calculated by the approach described in 13.4.1, except that a_{PC} (13.3.2.1) is used in place of a_o in Eq 5. If all values of $\%G_Q$ satisfy $15 \leq \%G_Q \leq 60$ and $\Delta s \leq 4$ mm [0.16 in.], then the candidate toughness is accepted. Otherwise, the results from this test are discarded and, if necessary, CC forces are modified appropriately for additional testing (2).

13.5 Toughness Determination—For any specimen where the candidate toughness is accepted (NPC or PC):

$$G_{IIC} = G_Q \quad (6)$$

13.6 To determine the value of a_{calc} (11.9.1.3), the compliance of the unloading line at the end of the NPC test (that is, after delamination growth has occurred, 11.9.1.2), is computed by a linear least squares regression analysis of the displacement versus force data using the method in Annex A3. The data shall be curve-fit over the same range of force as is used to obtain C_o (13.2.1). The compliance of the NPC test unloading line, C_u , is used in the equation:

$$a_{calc} = \left(\frac{C_u - A}{m} \right)^{1/3} \quad (7)$$

where A and m are the CC coefficients from the NPC test (13.2.1).

13.7 Statistics—For each series of tests, calculate the average value, standard deviation, and coefficient of variation (in percent) for each property determined:

$$\bar{x} = \left(\sum_{i=1}^n x_i \right) / n \quad (8)$$

$$S_{n-1} = \sqrt{\left(\sum_{i=1}^n x_i^2 - n \bar{x}^2 \right) / (n - 1)} \quad (9)$$

$$CV = 100 \times S_{n-1} / \bar{x} \quad (10)$$

where:

- \bar{x} = sample mean (average),
- S_{n-1} = sample standard deviation,
- CV = sample coefficient of variation, in percent,
- n = number of specimens, and
- x_i = measured or derived property.

14. Report

14.1 Report the following information, or report references pointing to other documentation containing this information, to the maximum extent applicable (reporting of items beyond the control of a given testing laboratory, such as might occur with

material details of panel fabrication parameters, shall be the responsibility of the requester):

NOTE 5—Guides E1309, E1434, and E1471 contain data reporting recommendations for composite materials and composite materials mechanical testing.

- 14.1.1 The revision level or date of issue of this test method;
- 14.1.2 The date(s) and location(s) of the test;
- 14.1.3 The name(s) of the test operator(s);
- 14.1.4 Any variations to this test method, anomalies noticed during testing, or equipment problems occurring during testing;
- 14.1.5 Identification of the material tested including: material specification, material type, material designation, manufacturer, manufacturer's lot or batch number, source (if not from manufacturer), date of certification, expiration of certification, filament diameter, tow or yarn filament count and twist, sizing, form or weave, fiber areal weight, matrix type, prepreg matrix content, and prepreg volatiles content;
- 14.1.6 Description of the fabrication steps used to prepare the laminate including: fabrication start date, fabrication end date, process specification, cure cycle, consolidation method, and a description of the equipment used;
- 14.1.7 Ply orientation (stacking sequence) of the laminate;
- 14.1.8 If requested, report density, reinforcement volume fraction, and void content test methods, specimen sampling method and geometries, test parameters, and test data;
- 14.1.9 Average ply thickness of the material;
- 14.1.10 Results of any nondestructive evaluation tests;
- 14.1.11 Method of preparing the test specimens, including specimen labeling scheme and method, specimen geometry, sampling method, coupon cutting method, identification of tab geometry, tab material, and tab adhesive used;
- 14.1.12 Calibration dates and methods for all measurement and test equipment;
- 14.1.13 Type of test machine, alignment data, and data acquisition sampling rate and equipment type;
- 14.1.14 Measured dimensions for each test specimen;
- 14.1.15 Conditioning parameters and results, and the procedure used if other than that specified in the test method;
- 14.1.16 Relative humidity and temperature of the testing laboratory;
- 14.1.17 Environment of the test machine environmental chamber (if used) and soak time at environment;
- 14.1.18 Loading and support nose type and dimensions for loading fixture, fixture roller diameters, r_1 and r_2 , and fixture span length, $2L$;
- 14.1.19 Number of specimens tested;
- 14.1.20 Speed of testing;
- 14.1.21 If applicable, transducer placement on the specimen, transducer type, and calibration data for each transducer used;
- 14.1.22 Tabulated data of force versus displacement, and force-displacement curves, for each specimen; and
- 14.1.23 Tabulated data of force versus displacement, and force-displacement curves for each system compliance test.

14.2 A set of recommended data sheets are given in **Appendix X1**. These sheets may be used as a template, but they are not intended to be inclusive to all items listed in 14.1. Thus,

additional data sheets may be required. The recommended data sheets contain the items listed below.

14.2.1 *Material*—Complete identification of the material tested, including prepreg manufacturer, material designation, manufacturing process, fiber volume fraction, and void content. Include the methods used to determine fiber volume fraction and void content.

14.2.2 *Coupon Data*—Type and thickness of insert, average width (B) and thickness ($2h$) of each specimen, and maximum width and thickness variation (as defined in 8.3.6) along the length of each specimen.

14.2.3 *Precracking Procedure*—Identification of whether the recommended procedure was used and, if not, complete description of the precracking process, and crack length versus width measurement procedure (11.9.3 and 13.3.2.1).

14.2.4 *Test Geometry*—Values of a_o used for NPC and PC tests, and values of a_1 and a_2 used for CC.

14.2.5 *Fixture Compliance*—Compliance of the test fixture as determined by the method of 7.2.3.

14.2.6 *Test Results*:

14.2.6.1 Force versus displacement curves from fracture tests indicating force and displacement at the maximum load point.

14.2.6.2 Values of m , A , and r^2 for each NPC and PC specimen tested.

14.2.6.3 Values of $\%G_Q$ for each NPC and PC specimen tested, with those results that were found to be unacceptable clearly indicated.

14.2.6.4 For cases where the recommended precracking procedure was not followed, the five measured values of crack length, the resulting value of a_{PC} , and the maximum measured difference in crack length along the delamination front of the precrack, Δs (13.3.2.1), for each PC test.

14.2.6.5 Tabulated results for those NPC and PC tests for which the candidate toughness was accepted indicating the test type (NPC or PC), the specimen number, the corresponding value of G_{IIc} , and the mean, normal standard deviation, and coefficient of variation (standard deviation divided by the mean, expressed as a percentage) for each data set (NPC and PC).

14.2.6.6 Other observations from testing that may have affected the test outcomes. Examples include, but are not limited to, specimen or manufacturing imperfections that are visually evident, relatively loud “cracking” noises well before crack advance, large amounts of nonlinearity in the loading curve, permanent deformation after unloading, a postmortem check that reveals tears, folds, or an irregular shape at the end of the insert (that is, the insert was not straight and parallel), deviation of the precrack from the midplane, occurrence of fiber-bridging, or sticking of the insert foil.

15. Precision and Bias⁵

15.1 *Interlaboratory Study*—An interlaboratory study (ILS) for precision data was conducted on this test method in 2011.

⁵ Supporting data have been filed at ASTM International Headquarters and may be obtained by requesting Research Report RR:D30-1006. Contact ASTM Customer Service at service@astm.org.

Nine laboratories participated in the evaluation of three material systems provided by a single supplier. Each laboratory tested two materials at ambient laboratory conditions. For a specific material, each laboratory was supplied with five test specimens. These were tested by a single operator. Each specimen was used to determine a single value of the non-precracked toughness and a single value of the precracked toughness. All specimen preparation, testing, and data reduction conformed to the requirements and specifications of this standard. Except for the limited number of materials that were tested, Practice E691 was followed for the design and analysis of the data.

15.1.1 Materials Considered:

15.1.1.1 IM7/977-3 Carbon/Epoxy, comprised of a continuous, high performance, intermediate modulus (276 GPa [40 msi]), PAN based carbon fiber and a 177 °C [350 °F] curing toughened epoxy resin with a 177 °C [350 °F] dry and 132 °C [270 °F] wet service capability.

15.1.1.2 G40-800/5276-1 Carbon/Epoxy, comprised of a continuous, high performance, intermediate modulus (290 GPa [42 msi]) carbon fiber and a highly toughened epoxy resin with a 177 °C [350 °F] curing temperature and a service temperature range of -59 to 121 °C [-75 to 250 °F].

15.1.1.3 S2/5216 Glass/Epoxy, comprised of S-2 glass fibers and a 93 to 121 °C [200 to 250 °F] curing modified epoxy resin with a service temperature range of -55 to 82 °C [-67 to 180 °F].

15.1.2 Test Specimens—For both the IM7/977-3 and G40-800/5276-1 materials, all specimens were cut from a single plate, whereas specimens were cut from two plates for S2/5216. Specimen thicknesses ($2h$) of the two carbon/epoxy materials were essentially the same with a mean value of 3.4 mm [0.134 in.], whereas the mean thickness of the glass/epoxy specimens was 4.1 mm [0.161 in.].

15.1.3 ILS Results—Key results from the ILS are presented in Table 2 and Table 3. Table 2 presents results from testing of non-precracked specimens, and Table 3 presents the precracked results. The first five columns of each table present the material name, the number of laboratories that participated in testing of that material, the total (combined) number of replicates tested by all participating laboratories, the mean

toughness obtained from all test results combined, and the average coefficient of variation (CV), obtained by averaging the CVs reported by each laboratory. The remaining columns present the repeatability (r) and reproducibility (R) limits that were obtained by statistical analyses of the data. Additional information is provided in Research Report RR:D30-1006.⁵

15.2 Precision—There are two types of precision: within-laboratory (the repeatability, r) and between-laboratory (the reproducibility, R). Practice E691 suggests that for a 95 % confidence interval the maximum difference between an individual observation and the average should be within 2.0 standard deviations, while the maximum difference between any two observations should be within 2.8 standard deviations. The final four columns of Table 2 and Table 3 present the latter forms of r and R only, as the former can be derived from these. That is, two test results that are obtained (by the same operator using the same equipment on the same day) from an individual laboratory for the same material shall be judged not equivalent if they differ by more than the “ r ” value for that material; two test results obtained by different operators using different equipment in different laboratories shall be judged not equivalent if they differ by more than the “ R ” value for that material. Repeatability and reproducibility limits for comparisons between individual observations and mean values may be obtained by multiplying the values in the last four columns of Table 2 and Table 3 by 2.0/2.8. The results of Table 2 and Table 3 indicate that the precision of this test method is relatively insensitive to minor variations in testing practices.

NOTE 6—Due to the number of participating laboratories and materials and specimens tested, the repeatability and reproducibility limits of Table 2 and Table 3 should be considered as general guides, and the associated 95 % probabilities as only a rough indicator of what can be expected.

NOTE 7—To judge the equivalency of two test results of materials different than those in Table 2 and Table 3, it is recommended to choose the material from the table that is closest in characteristics to the test material.

15.3 Bias—No other test method for determining the mode II interlaminar fracture toughness of composite laminates has been evaluated to the extent where it can be used to determine inherent bias in the ENF test.

TABLE 2 Non-Precracked Results from ILS

Material	No. Labs	Total Replicates	Mean G_{IIc} (kJ/m ²) [in.-lbf/in. ²]	Mean CV (%) ^A	r (kJ/m ²) [in.-lbf/in. ²]	r (% of mean)	R (kJ/m ²) [in.-lbf/in. ²]	R (% of mean)
IM7/977-3	4	20	0.908 [5.18]	3.1	0.0836 [0.477]	9.2	0.0871 [0.497]	9.6
G40-800/5276-1	5	25	2.11 [12.0]	3.9	0.246 [1.40]	11.6	0.285 [1.63]	13.5
S2/5216	9	44	1.17 [6.68]	6.5	0.222 [1.27]	19.0	0.222 [1.27]	19.0

^A Average of the coefficients of variation reported by each participating lab.

16. Keywords

16.1 composite materials; delamination; end notched flexure; ENF; interlaminar fracture toughness; mode II; shear

TABLE 3 Precracked Results from ILS

Material	No. Labs	Total Replicates	Mean G_{IIc} (kJ/m ²) [in.-lbf/in. ²]	Mean CV (%) ^A	r (kJ/m ²) [in.-lbf/in. ²]	r (% of mean)	R (kJ/m ²) [in.-lbf/in. ²]	R (% of mean)
IM7/977-3	4	20	0.620 [3.54]	5.4	0.103 [0.588]	16.6	0.105 [0.600]	17.0
G40-800/5276-1	5	25	1.99 [11.4]	3.8	0.219 [1.25]	11.0	0.239 [1.36]	12.1
S2/5216	9	43	0.930 [5.31]	5.9	0.159 [0.908]	17.1	0.188 [1.07]	20.2

^A Average of the coefficients of variation reported by each participating lab.

ANNEXES

(Mandatory Information)

A1. CRITICAL FORCE AND FLEXURAL MODULUS ESTIMATION

A1.1 Overview

A1.1.1 Values of the mode II fracture toughness and flexural modulus, E_{If} , for the material of interest are required in order to estimate the critical force, P_c . The flexural modulus may be obtained using Test Method **D7264/D7264M** or, although somewhat less accurate, the longitudinal modulus, E_{II} , may be used in its place. E_{If} may also be determined from CC data using the method described in **A1.2.2**. Initial estimates of G_{IIc} may be obtained from data on similar composite systems, from previous testing experience on the material of interest, or from an “exploratory test” as described in **A2.1**.

A1.2 Calculation

A1.2.1 The critical force at fracture can be approximated using classical beam theory (CBT) as **(1)**:

$$P_c = \frac{4B}{3a_o} \sqrt{G_{IIc} E_{If} h^3} \quad (\text{A1.1})$$

A1.2.2 *Flexural Modulus*—If E_{If} is to be extracted from the results of a test, CBT yields **(1)**:

$$E_{If} = \frac{L^3}{4ABh^3} \quad (\text{A1.2})$$

where A is the CC coefficient obtained during CC testing of that specimen.

A2. FORCE DETERMINATION FOR COMPLIANCE CALIBRATION

A2.1 Overview

A2.1.1 Values of G_{IIc} and E_{If} are required in order to determine the force for compliance calibration and are to be obtained by one of the methods described in **Annex A1**. Note that proper choice of the CC forces will affect whether or not the candidate toughness, G_Q , is acceptable. Thus, in certain cases, the first test of a new material will produce a value of G_Q that is not acceptable. When this occurs, this first test (NPC and/or PC) can be classified as “exploratory,” the value of G_Q that was obtained can be used as an improved approximation for G_{IIc} , the value of E_{If} may be extracted from the test data as described in **A1.2.2**, and these values of G_{IIc} and E_{If} can be used to determine new values for the CC forces. Further, it is recommended that the data from the first test of a new material

that produces an acceptable value of G_Q are used to update the CC forces for subsequent testing of that material.

A2.2 Calculation

A2.2.1 Peak forces during CC are determined using CBT as $0.5P_c$ at each crack length. This is chosen to produce a value of G at each crack length that is 25 % of G_{IIc} . This yields: **(1, 4)**

$$P_j = \frac{2B}{3a_j} \sqrt{G_{IIc} E_{If} h^3} \quad (\text{A2.1})$$

where P_j is the peak value of the force to be used during CC at a_j , and a_j is the j^{th} crack length used during CC. For each NPC and PC test there are two CC forces and two associated crack lengths: $a_1 = 20 \text{ mm [0.8 in.]}$ and $a_2 = 40 \text{ mm [1.6 in.]}$.

A3. LINEAR LEAST SQUARES REGRESSION ANALYSIS

A3.1 Overview

A3.1.1 Linear least squares regression analyses are used to obtain the compliance, C , from the displacement versus force data at any crack length (13.2.1, 13.2.2, and 13.6). They are also used to obtain the CC coefficients that define the equations for non-precracked and precracked compliance versus crack length (13.2.1 and 13.2.2). The equations that follow are standard expressions and should correspond to those used in commercially available software packages that fit a linear equation to a set of data. However, this should be verified, and the equations defined herein are to be utilized in the event of any differences.

A3.2 Calculation

A3.2.1 Consider a set of n data points (x_i, y_i) that are to be curve-fit with a linear equation of the form $y = bx + d$. Thus, when fitting displacement versus force (δ vs P) data, (x_i, y_i) correspond to the discrete values of (P_i, δ_i) , and b will correspond to the compliance at that crack length. When fitting

compliance versus crack length (C vs a) data to Eq 2, (x_i, y_i) correspond to the discrete values of (a_i^3, C_i) , b will correspond to the slope, m , and d is the intercept A . A linear least squares regression analysis minimizes the sum of the squared residuals, where a residual is defined as the difference between the curve-fit ($y = bx + d$) and the actual data point at each known value of the independent variable. Applying this criterion results in the following equations:

$$b = \frac{n \sum x_i y_i - \sum x_i \sum y_i}{n \sum x_i^2 - (\sum x_i)^2} \quad (\text{A3.1})$$

$$d = \frac{\sum y_i - m \sum x_i}{n} \quad (\text{A3.2})$$

The correlation coefficient, r^2 , is given by:

$$r^2 = \frac{(n \sum x_i y_i - \sum x_i \sum y_i)^2}{[n \sum x_i^2 - (\sum x_i)^2][n \sum y_i^2 - (\sum y_i)^2]} \quad (\text{A3.3})$$

All summations in Eq A3.1-A3.3 are taken over the range $i = 1$ to n .

APPENDIX

(Nonmandatory Information)

X1. RECOMMENDED DATA SHEETS

X1.1 Recommended Data Sheets

X1.1.1 Data Sheets

Panel Data			
Material	Producer	Date of manufacture	Date of cutting into specimens
Panel No.	Specimen numbers from this panel		
Insert material	Insert thickness	FAW	Vf

FIG. X1.1 Panel Data Sheet



Specimen Geometry for Panel No:						Material:							
Date of measurement:						Operator:							
Specimen Width and Thickness Data						Thickness, 2h (mm)							
Specimen Number	Width, B (mm)					Location 1		Location 2		Location 3		Avg.	Δ Max.
	Loc. 1	Loc. 2	Loc. 3	Avg.	Δ Max.	Left	Right	Left	Right	Left	Right		
XX-YY-01 XX-YY-02													
Mean values													

FIG. X1.2 Specimen Geometry Sheet (SI Units)

Specimen Geometry for Panel No:						Material:							
Date of measurement:						Operator:							
Specimen Width and Thickness Data						Thickness, 2h (in.)							
Specimen Number	Width, B (in.)					Location 1		Location 2		Location 3		Avg.	Δ Max.
	Loc. 1	Loc. 2	Loc. 3	Avg.	Δ Max.	Left	Right	Left	Right	Left	Right		
XX-YY-01 XX-YY-02													
Mean values													

FIG. X1.3 Specimen Geometry Sheet (Inch-Pound Units)

Non-Precracked Test Results															
Material		Date of Tests		Operator		a_0 (mm):		a_1 [a_{\min} for CC] (mm):		a_2 [a_{\max} for CC] (mm):		r_1 (mm)	r_2 (mm)		
DATA															
Spec. No.	CC loads (N)		Compliances (mm/N)			A (mm/N)	m $1/(Nmm^2)$	r^2	P_{\max} (N)	G_Q (kJ/m ²)	%G _Q ($a=a_1$)	%G _Q ($a=a_2$)	Accept? (Y/N)	G_{IIC} (kJ/m ²)	a_{calc} (mm)
	At a_1	At a_2	$C(a_1)$	$C(a_2)$	$C(a_0)$										
XX-YY-01 XX-YY-02															
											Mean SD CV No. Spec. Max Min				

FIG. X1.4 ENF Standard Non-Precracked Test Data Reporting Sheet (SI Units)



Non-Precracked Test Results															
Material	Date of Tests		Operator		a_0 (in.):		a_1 [a_{min} for CC] (in.):		a_2 [a_{max} for CC] (in.):		r_1 (in.)	r_2 (in.)			
DATA															
Spec. No.	CC loads (lbf)		Compliances (in./lbf)			A (in./lbf)	m 1/(lbf-in. ²)	r^2	P_{Max} (lbf)	G_Q (in.-lbf/in. ²)	% G_Q ($a=a_1$)	% G_Q ($a=a_2$)	Accept? (Y/N)	G_{IIC} (in.-lbf/in. ²)	a_{calc} (in.)
	At a_1	At a_2	C(a_1)	C(a_2)	C(a_0)										
XX-YY-01 XX-YY-02															
												Mean SD CV No. Spec. Max Min			

FIG. X1.5 ENF Standard Non-Precracked Test Data Reporting Sheet (Inch-Pound Units)

Precracked Test Results														
Material	Date	Operator:		a_0 (mm):		a_1 [a_{min} for CC] (mm):		a_2 [a_{max} for CC] (mm):		r_1 (mm)	r_2 (mm)			
Description of precracking method:														
DATA														
Spec. No.	CC loads (N)		Compliances (mm/N)			A (mm/N)	m 1/(Nmm ²)	r^2	P_{Max} (N)	G_Q (kJ/m ²)	% G_Q ($a=a_1$)	% G_Q ($a=a_2$)	Accept? (Y/N)	G_{IIC} (kJ/m ²)
	At a_1	At a_2	C(a_1)	C(a_2)	C(a_0)									
XX-YY-01 XX-YY-02														
												Mean SD CV No. Spec. Max Min		

FIG. X1.6 ENF Standard Precracked Test Data Reporting Sheet (SI Units)

Precracked Test Results														
Material	Date	Operator:	a_0 (in.):			a_1 [a_{\min} for CC] (in.):		a_2 [a_{\max} for CC] (in.):		r_1 (in.)	r_2 (in.)			
Description of precracking method:														
DATA														
Spec. No.	CC loads (lbf)		Compliances (in./lbf)			A (in./lbf)	m 1/(lbf-in. ²)	r^2	P_{\max} (lbf)	G_Q (in.-lbf/in. ²)	% G_Q ($a=a_1$)	% G_Q ($a=a_2$)	Accept? (Y/N)	G_{IIC} (in.-lbf/in. ²)
	At a_1	At a_2	$C(a_1)$	$C(a_2)$	$C(a_0)$									
XX-YY-01														
XX-YY-02														
												Mean SD CV No. Spec. Max Min		

FIG. X1.7 ENF Standard Precracked Test Data Reporting Sheet (Inch-Pound Units)

Fixture compliance (mm/N) per 7.2.3:

Minimum specimen compliance (mm/N) from tabulated results:

Ratio of fixture compliance to minimum specimen compliance: $\leq 0.03?$ (Y/N) Acceptable? (Y/N)

Fixture compliance (in./lbf) per 7.2.3:

Minimum specimen compliance (in./lbf) from tabulated results:

Ratio of fixture compliance to minimum specimen compliance: $\leq 0.03?$ (Y/N) Acceptable? (Y/N)

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